

Section-A

- 1.) Write a short note on Initial Value Problems.
- 2.) Find the interval in which the root of eqn. $x^3 - x - 11 = 0$ lies.
- 3.) Write various techniques for approximating interpolating polynomials.
- 4.) Write formula of Modified Euler's method for O.D.E.
- 5.) Write two lines of regression by principle of Least Square.
- 6.) Define Karl Pearson's Coefficient of Correlation.
- 7.) Write an example of Civil Engineering related real life problem.
- 8.) Write Normal equations for fitting of straight line.
- 9.) Write relation b/w Forward operator and Shift operator.
- 10.) Write three different techniques for the solution of Boundary Value Problem.
- 11.) Define Interpolation & Extrapolation.
- 12.) Evaluate $\Delta^n(e^x)$, the interval of difference being unity.
- 13.) Find a Forward Difference table for the data:

$x :$	1	2	3	4	5
$y :$	25	88	125	250	300
- 14.) Evaluate $\Delta^n(e^{3x+5})$.
- 15.) What is meant by saying that Runge-Kutta formula is of the fourth order?
- 16.) Find the root of the equation $x \sin x + \cos x = 0$
- 17.) What are Positive & Negative Correlation?
- 18.) Write the formula of Euler's Method.
- 19.) What is Milne-Simpson Method?
- 20.) What are Regression Equations?

Section-B

- 1.) By the Method of Least Squares, find the straight line that best fits the following data:

$x :$	1	2	3	4	5
$y :$	14	27	40	55	68

2) Using Runge-Kutta method of order 4, find $y(0.2)$ for the eqn:

$$\frac{dy}{dx} = \frac{y-x}{y+x}, \quad y(0)=1, \quad \text{take } h=0.2.$$

3) Given the following experimental values:

$x: 0 \quad 1 \quad 2 \quad 3$

$y: 2 \quad 4 \quad 10 \quad 15$

Fit by the method of Least Square a parabola of the type

$$y = a + bx^2.$$

4) Calculate the Coeff. of correlation & obtain the least square regression lines for the following data:

$x: 1 \quad 2 \quad 3 \quad 4 \quad 5 \quad 6 \quad 7 \quad 8 \quad 9$

$y: 9 \quad 8 \quad 10 \quad 12 \quad 11 \quad 13 \quad 14 \quad 16 \quad 15$

5) Use Galerkin's method of least square to find the app. solⁿ of B.V.P $x \frac{d^2y}{dx^2} + \frac{dy}{dx} + y = x$, $y(0)=0$; $y(1)=1$

6) Using Taylor's Series Method, find the solution of $\frac{dy}{dx} = 3x + y^2$ where $y(0)=1$. Find the value of 'y' at $x=0.01$.

7) Find the value of 'y' at $x=0.2$, Given that $\frac{dy}{dx} = x^2 + y$, $y(0)=1$ in two steps of 0.1 each by using Euler's modified Method.

8) Find the cubic polynomial which takes the values: $y(0)=1$, $y(1)=0$, $y(2)=1$ & $y(3)=10$ Hence or otherwise obtain $y(4)$.

9) Given $x: 0 \quad 1 \quad 2 \quad 3 \quad 4$ Evaluate $f(3.8)$.
 $f(x): 1.00 \quad 1.50 \quad 2.20 \quad 3.10 \quad 4.60$

10) Find the population of town in 1962. Given that

Year: 1947 1957 1967 1977 1987

Population: 15 20 27 39 52

using Gauss's Forward difference formula.

Section C

1) Solve the equation ~~for~~ $y'' = x+y$ with the boundary conditions $y(0) = y(1) = 0$

2) Using Runge Kutta Method of fourth order, solve $\frac{dy}{dx} = \frac{y-x^2}{y^2+x^2}$ with $y(0) = 1$ at $x = 0.2, 0.4$.

3) Supplement Lagrange's Interpolation formula & use it to compute the value of $f(5)$ from the following data for x & $f(x)$:
(2, 46), (7, 71), (10, 110).

4) Solve the problem $\frac{dy}{dx} = -2y+x$, $y(0) = 1$ for $y(0.1), y(0.2)$ by using a) Runge Kutta of third order
b) Runge Kutta method of fourth order.

5) Fit a parabola $y = a+bx+cx^2$ to the data

x:	0	1	2	3	4
y:	1	1.8	1.3	2.5	6.3

6) Given $\sin 45^\circ = 0.7071$, $\sin 50^\circ = 0.7660$, $\sin 55^\circ = 0.8192$, $\sin 60^\circ = 0.8660$. Find $\sin 52^\circ$ using Newton's forward formula.

7) Using Lagrange's Interpolation formula, find $y(10)$ from the table:

x: 5 6 9 11

y: 12 13 14 16

8) Explain New-Marks Method.

9) Apply Euler's Method to solve $\frac{dy}{dx} = \frac{y-x}{y+x}$ at $x=0.1$ given that $y(0) = 1$

10) Use Midrule Simpson Method to the eqn. $\frac{dy}{dx} = x+y$, $y(0) = 1$ & find the values of 'y' at $x=0.4$ & 0.5 ($h=0.1$).